

7th M4DT Day - SIM

Reliability Through Digitalization of Traceable Data

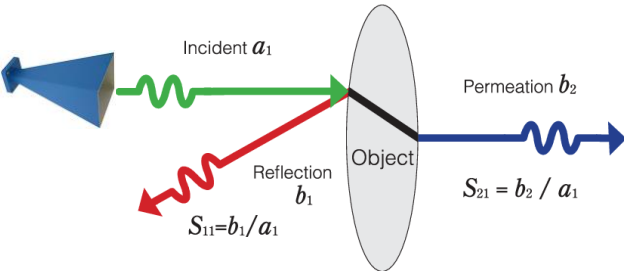
JULY | 2021

Guillermo Monasterios

RF & Microwave Metrology



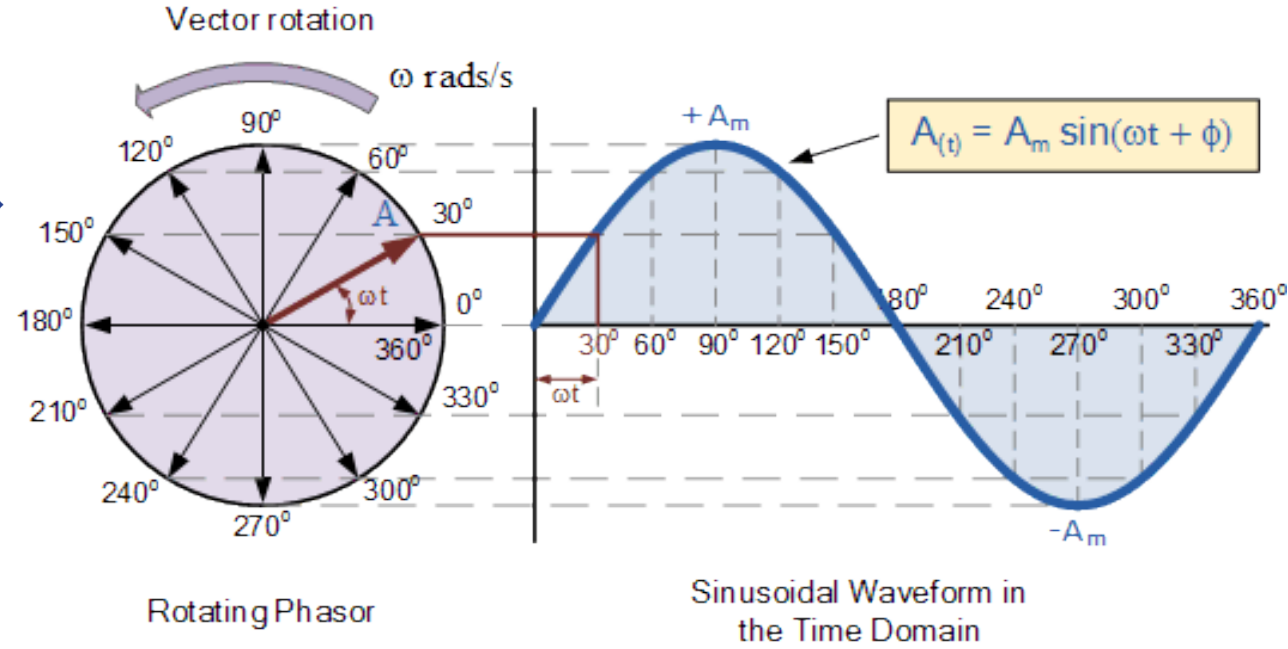
Graphical Representation of a Wave:



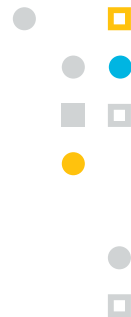
$$S_{11} = \frac{\text{reflected}}{\text{incident}}$$

$$S_{21} = \frac{\text{transmitted}}{\text{incident}}$$

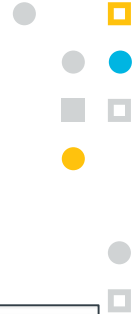
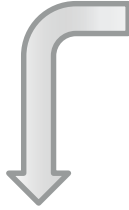
S-parameters: n^2



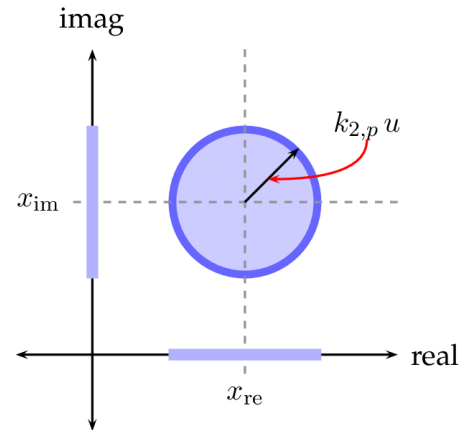
Frequency (GHz)	S1,1 Zr: 50 Ω Real	S1,1 Zr: 50 Ω Imag
1,000	0,005	0,001



Frequency (GHz)	S1,1 Zr: 50 Ω Real	S1,1 Zr: 50 Ω Imag
1,000	0,005	0,001



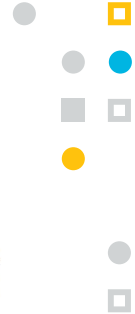
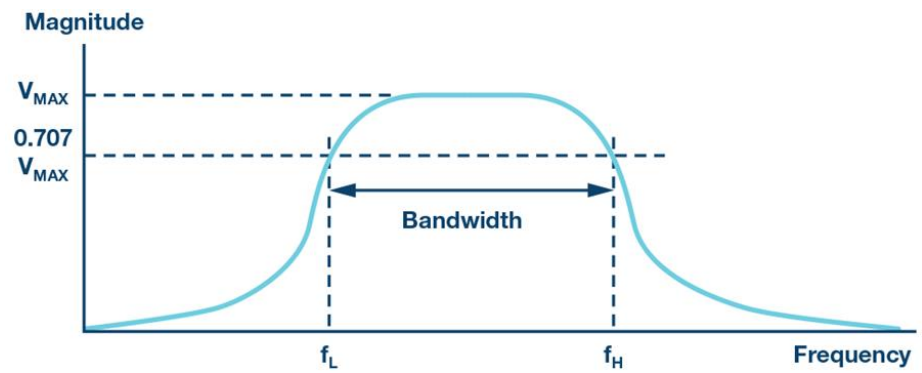
Frequency (GHz)	S1,1 Zr: 50 Ω Real	S1,1 Zr: 50 Ω u(Real)	S1,1 Zr: 50 Ω Imag	S1,1 Zr: 50 Ω u(Imag)
1,000	0,005	0,003	0,001	0,003



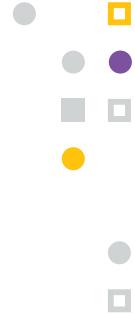
2 port example:

Band-pass filter

S-parameters: 4

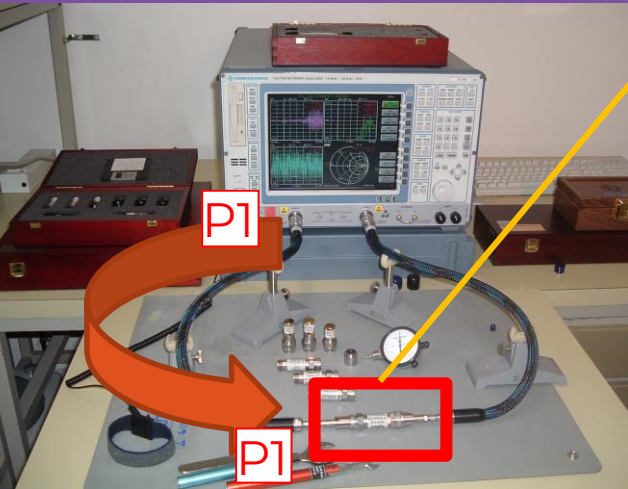


Frequency (GHz)	S1,1 Zr: 50 Ω Real	S1,1 Zr: 50 Ω Imag	S2,1 Zr: 50 Ω Real	S2,1 Zr: 50 Ω Imag	S1,2 Zr: 50 Ω Real	S1,2 Zr: 50 Ω Imag	S2,2 Zr: 50 Ω Real	S2,2 Zr: 50 Ω Imag
1,000	0,005	0,001	0,027	-0,100	0,027	-0,100	0,004	0,000
1,500	0,006	-0,001	-0,039	-0,096	-0,039	-0,096	0,004	-0,001
2,000	0,004	-0,002	-0,089	-0,053	-0,089	-0,052	0,002	-0,004
2,500	0,001	-0,002	-0,102	0,012	-0,102	0,012	-0,001	-0,003
3,000	-0,002	-0,001	-0,074	0,071	-0,074	0,071	-0,003	0,001
3,500	-0,005	0,002	-0,016	0,101	-0,016	0,101	-0,001	0,006
4,000	-0,007	0,007	0,049	0,090	0,049	0,090	0,004	0,008
4,500	-0,007	0,013	0,093	0,042	0,093	0,042	0,010	0,005
5,000	-0,002	0,018	0,100	-0,023	0,099	-0,024	0,013	-0,001
5,500	0,005	0,020	0,065	-0,079	0,065	-0,079	0,010	-0,008
6,000	0,012	0,019	0,003	-0,102	0,003	-0,102	0,002	-0,011
6,500	0,019	0,014	-0,060	-0,083	-0,060	-0,083	-0,006	-0,008
7,000	0,024	0,006	-0,098	-0,029	-0,098	-0,029	-0,010	0,000

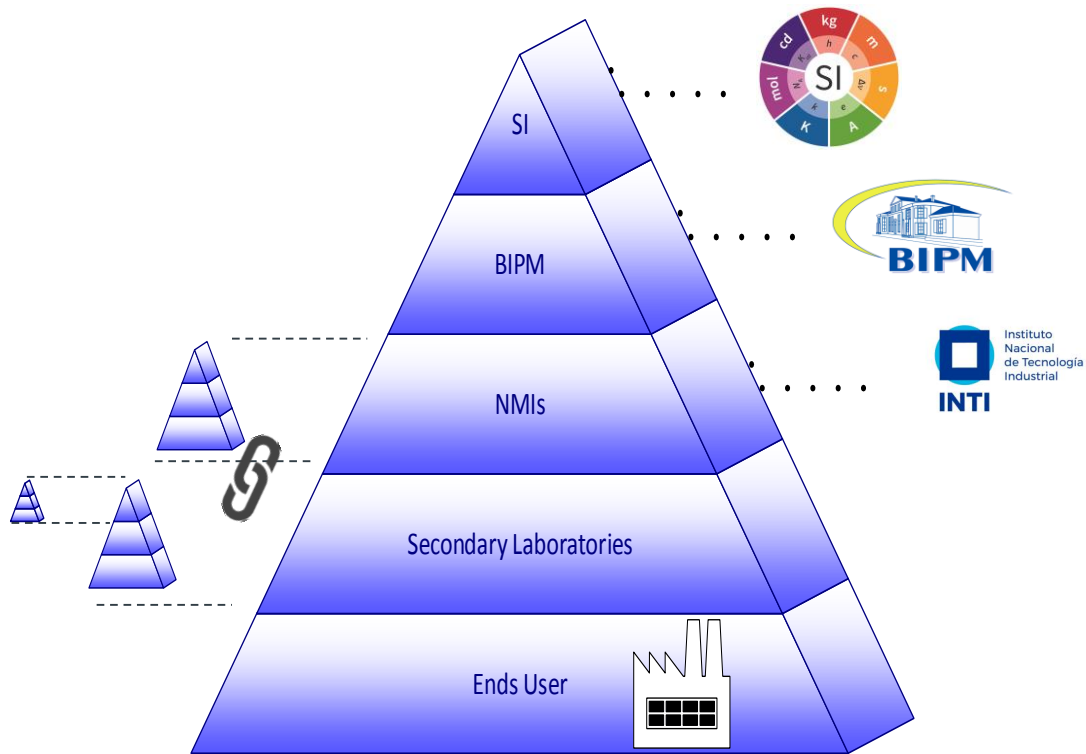


Correlations between ...

- Real/Imaginary parts
- Real/Imaginary parts at different frequencies
- Different S-parameters
- Different DUTs
- Uncertainty components
- Measured values vs. temperature, humidity, time.

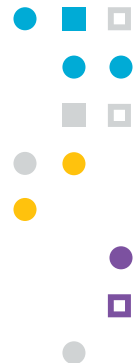
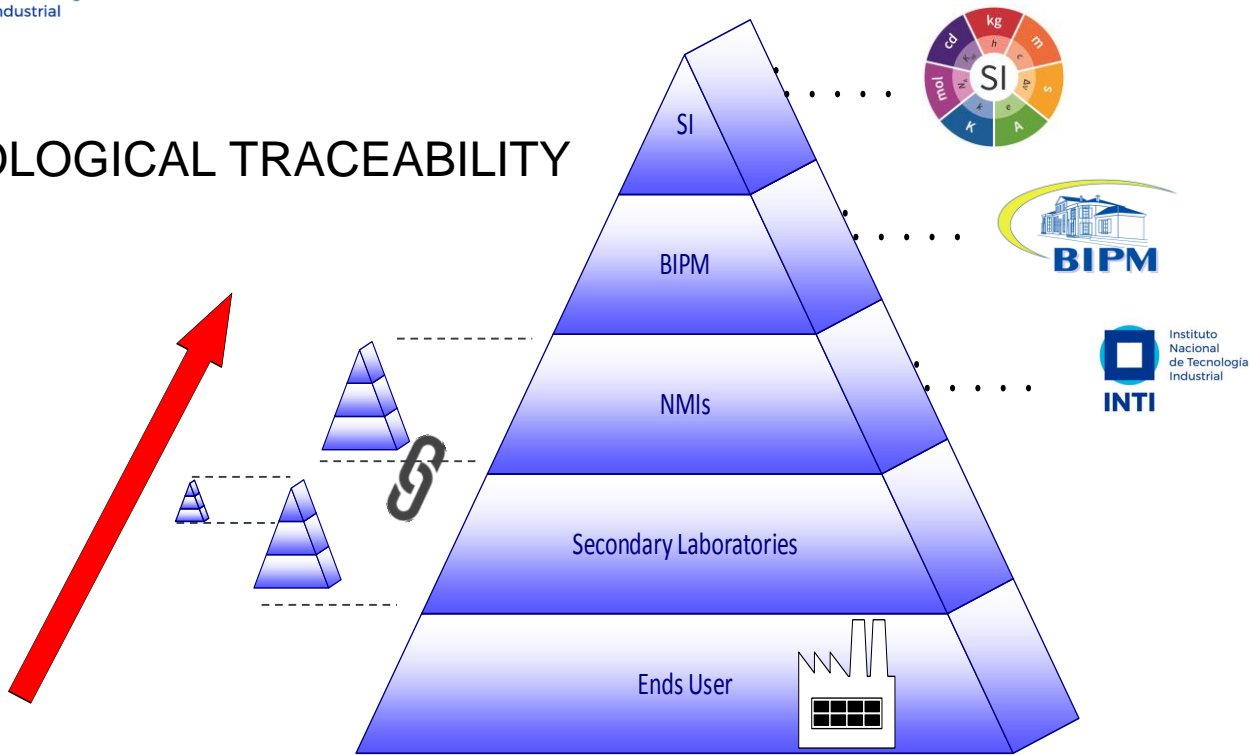


Traceability pyramid



Traceability pyramid

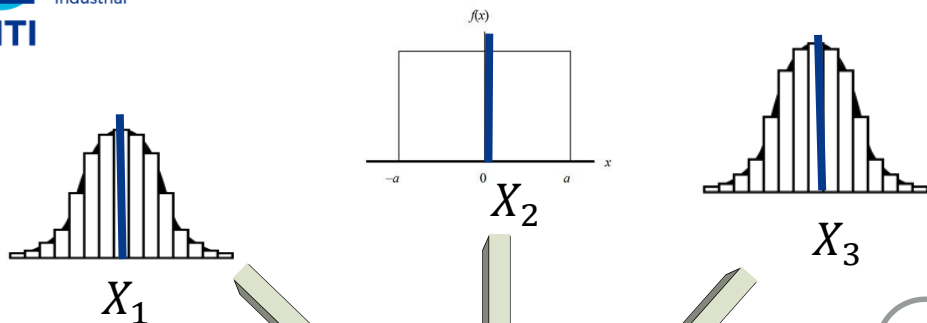
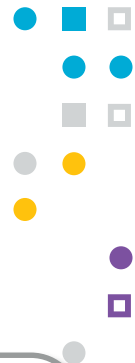
METROLOGICAL TRACEABILITY



[VIM3] 2.41


property of a **measurement result** whereby the result can be related to a reference through a documented unbroken chain of calibrations, each contributing to the measurement uncertainty

set of **quantity values** being attributed to a **measurand** together with any other available relevant information

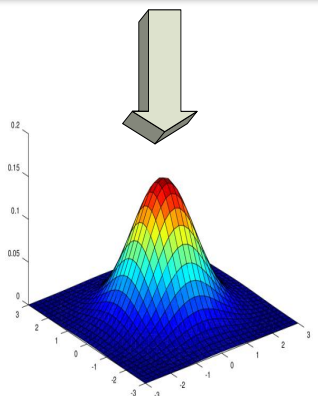


Influence quantities (x_i)

Measurement model $f(x_i)$

Interaction between measurand and uncertainty in the same expression. 

$S_{11} = \frac{\textit{reflected}}{\textit{incident}}$



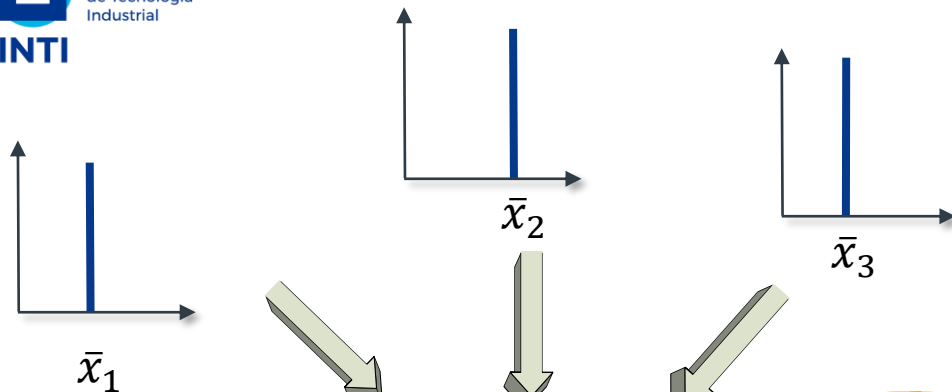
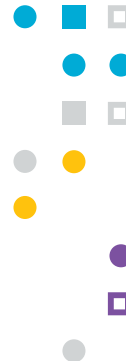
$Y = y \pm U(y)$

i.e.: Value=1 ; unc.= 0.001
 $f'(x_i) = 1 \times (1 \pm 0.001) = ?$

Multivariate case



LPU

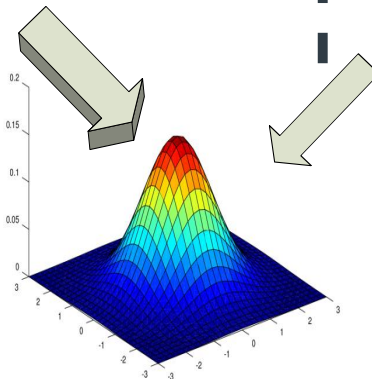
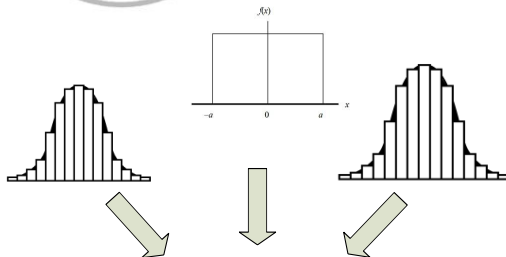


Measurement model $f(x_i)$

Uncertainty model $f(u_{x_i})$

Sensitivity coefficients

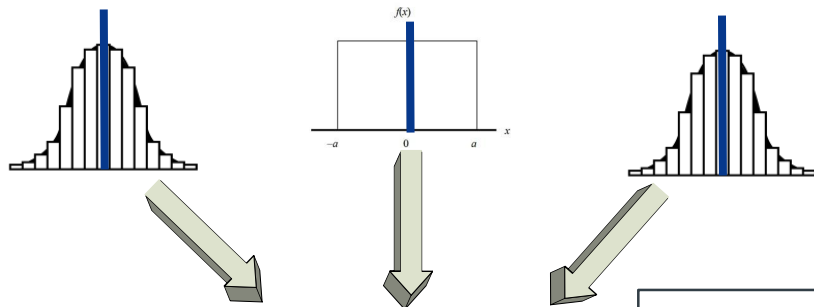
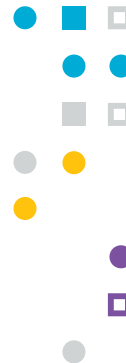
$$S_{11} = \frac{\text{reflected}}{\text{incident}}$$



$$Y = y \pm U(y)$$

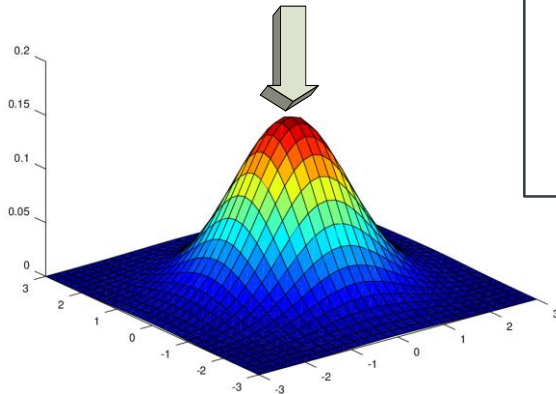


Rigorous method



Measurement model $f(xi)$

$$S_{11} = \frac{\text{reflected}}{\text{incident}}$$



$$S_{11} = \frac{\frac{S_{11}^m - N_L}{N_{HL}} - E'_{00} - kC_{00}E'_{01}}{(C_{11} + kC_{01}C_{10}E'_{11}) \left(\frac{S_{11}^m - N_L}{N_{HL}} - E'_{00} - kC_{00}E'_{01} \right) + k^2 C_{10}C_{01}E'_{01}}$$

$$E'_{00} = E_{00} + D_{00}$$

$$E'_{01} = E_{01}D_{01}$$

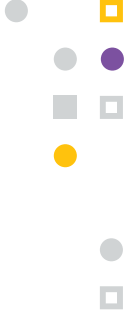
$$E'_{11} = E_{11} + D_{11}$$

$$k = \frac{1}{1 - E'_{11}C_{00}}$$





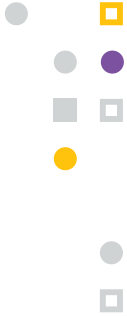
Issues /Solutions

- **Different models**  **Only 1 model (rigorous method)**



Issues /Solutions

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- **Mixed data types**  **Uncertainty objects**



Issues /Solutions

- Different models  Only 1 model (rigorous method)
- **Mixed data types**  **Uncertainty objects**

Case 1:

Measured voltaje: $V = 5V$

$U(V) = 1\mu V$

Calibration
certificate

Uncertainty object

$V = (5, 1e-6)$

Case 2:

Measured voltaje:

$V = (5, 0)$

$U(V) = (0, 1e-6)$ Additive uncertainty

$U(V) = (1, 1e-6)$ Multiplicative uncertainty

Command Window

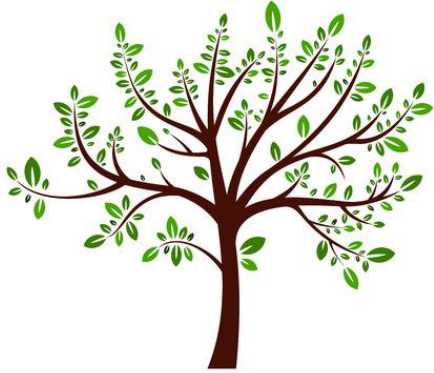
```
>> v = unc(5, 1e-6)
```



```
v =
```

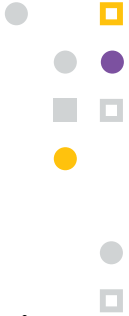
```
(5 ± 1e-06)
```

```
fx >>
```

Issues /Solutions



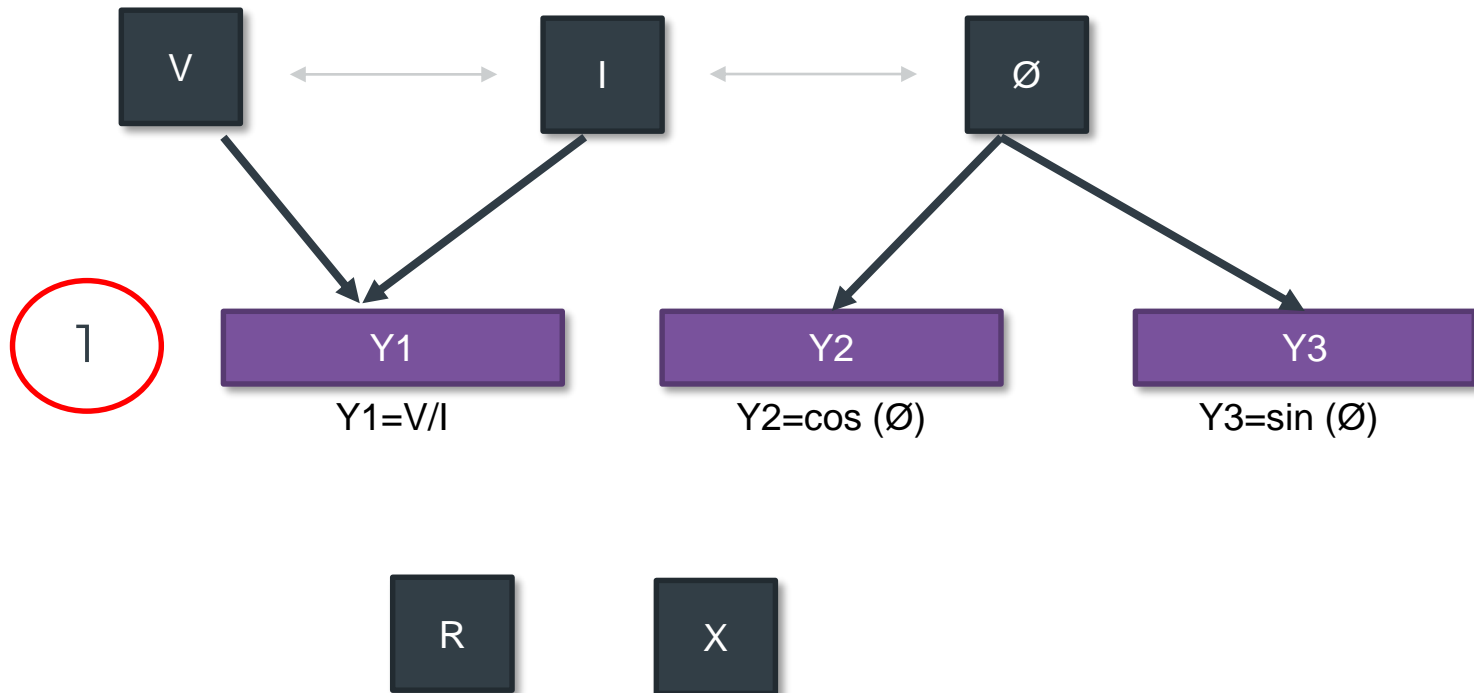
- Different models  Only 1 model (rigorous method)
- Mixed data types  Uncertainty objects
- **Complicated calculations** **Automatic uncertainty propagation through automatic differentiation**



$$R = \frac{V}{I} \cos \phi$$

$$X = \frac{V}{I} \sin \phi$$

MEASUREMENT MODEL

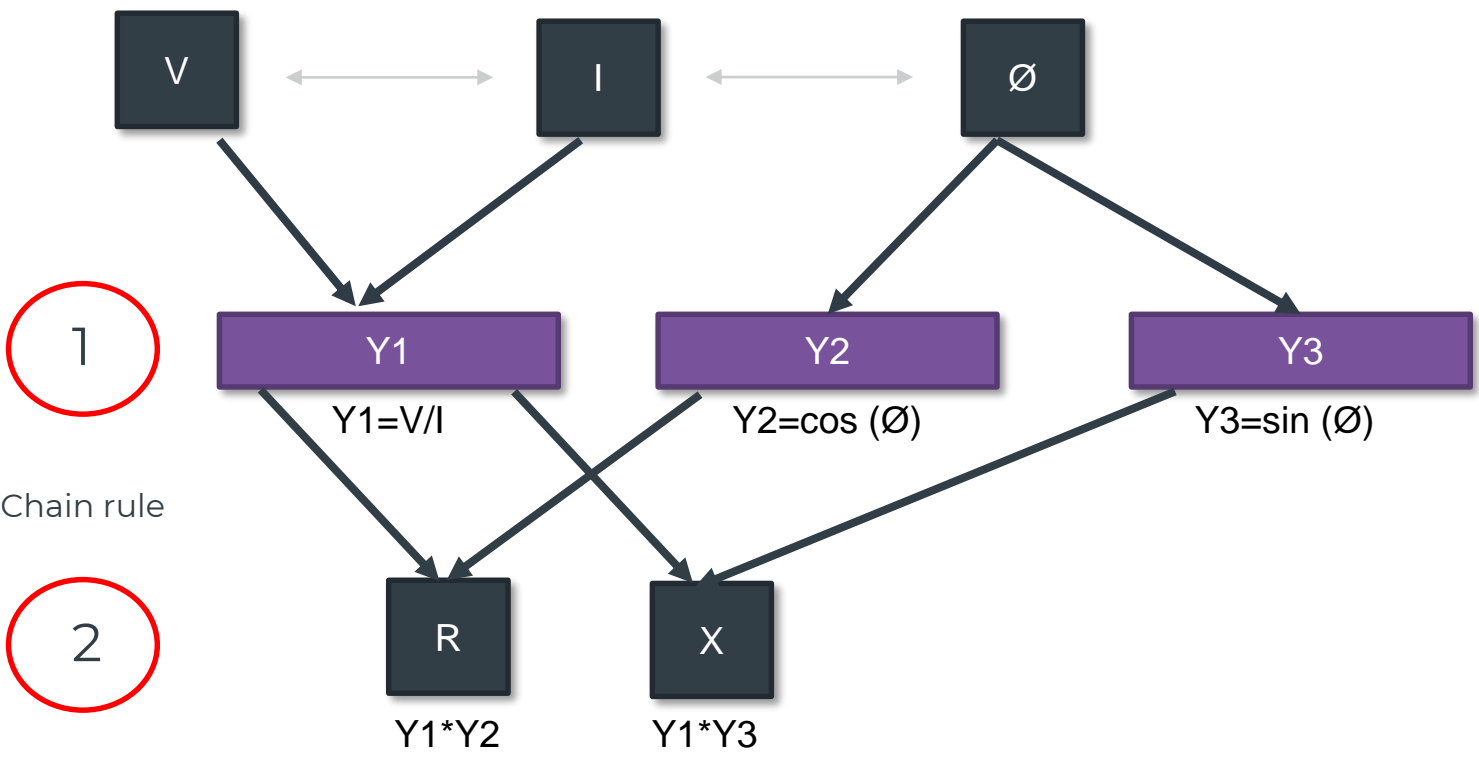
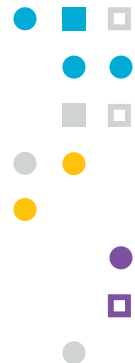


Graphical decomposition of a measurement model

$$R = \frac{V}{I} \cos \phi$$

$$X = \frac{V}{I} \sin \phi$$

MEASUREMENT MODEL



1

Chain rule

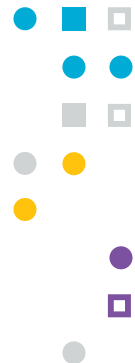
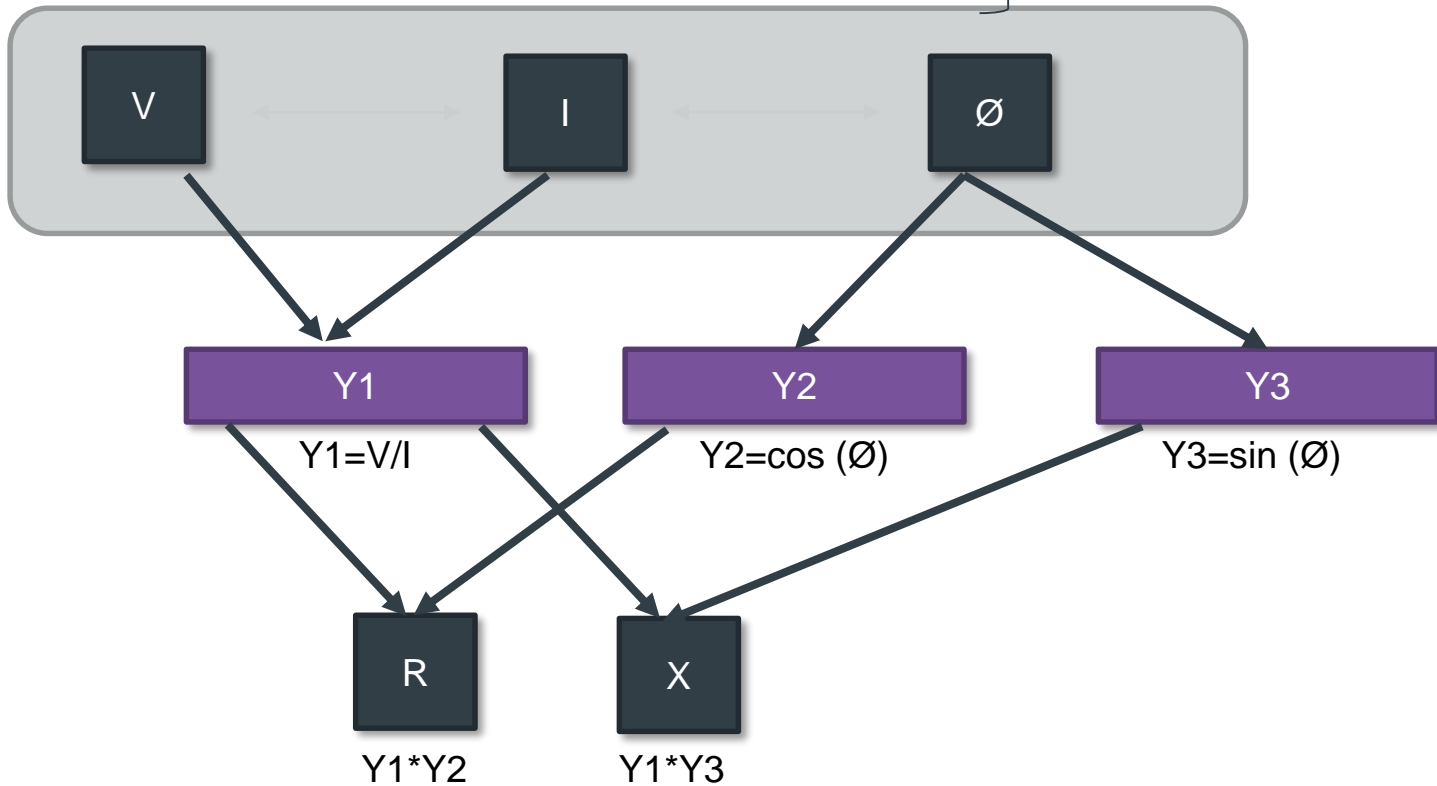
2

Graphical decomposition of a measurement model

$$R = \frac{V}{I} \cos \phi$$

$$X = \frac{V}{I} \sin \phi$$

MEASUREMENT MODEL

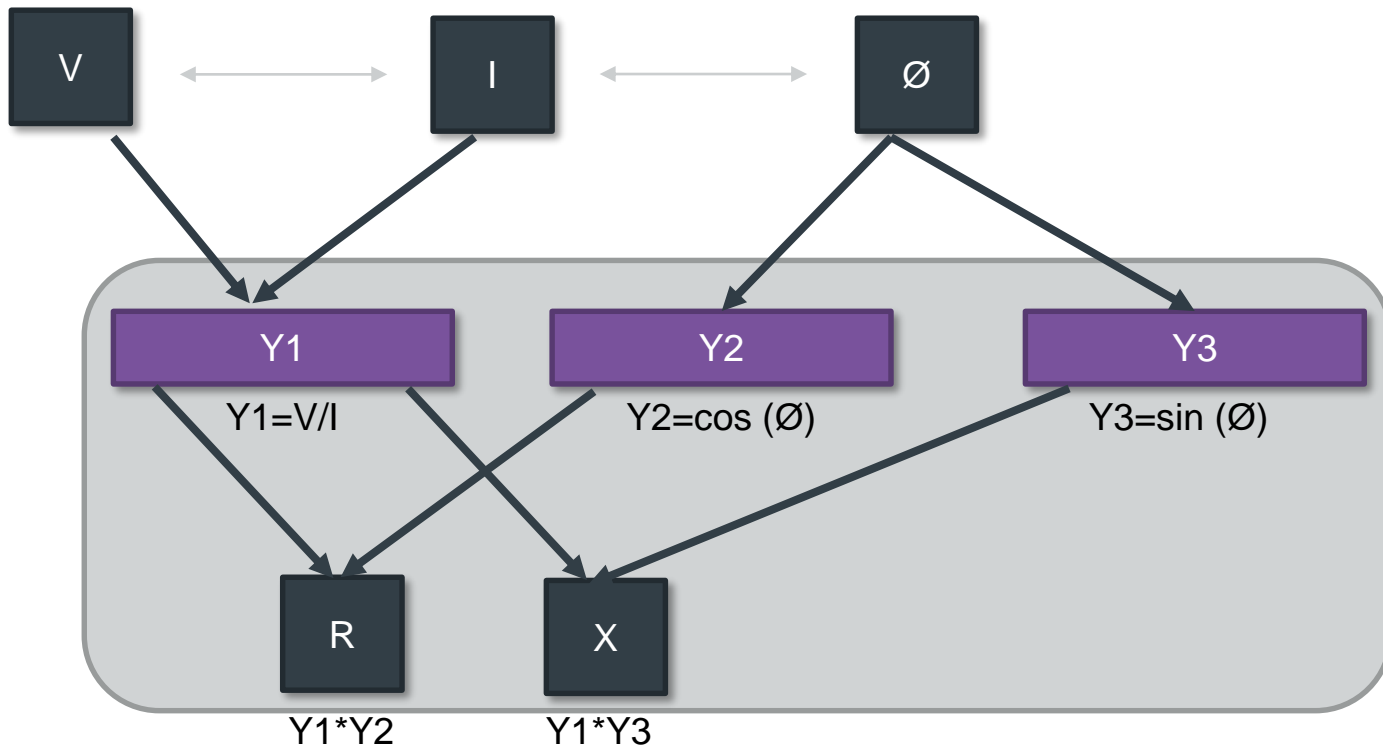
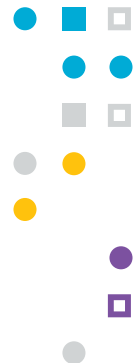


Graphical decomposition of a measurement model

$$R = \frac{V}{I} \cos \phi$$

$$X = \frac{V}{I} \sin \phi$$

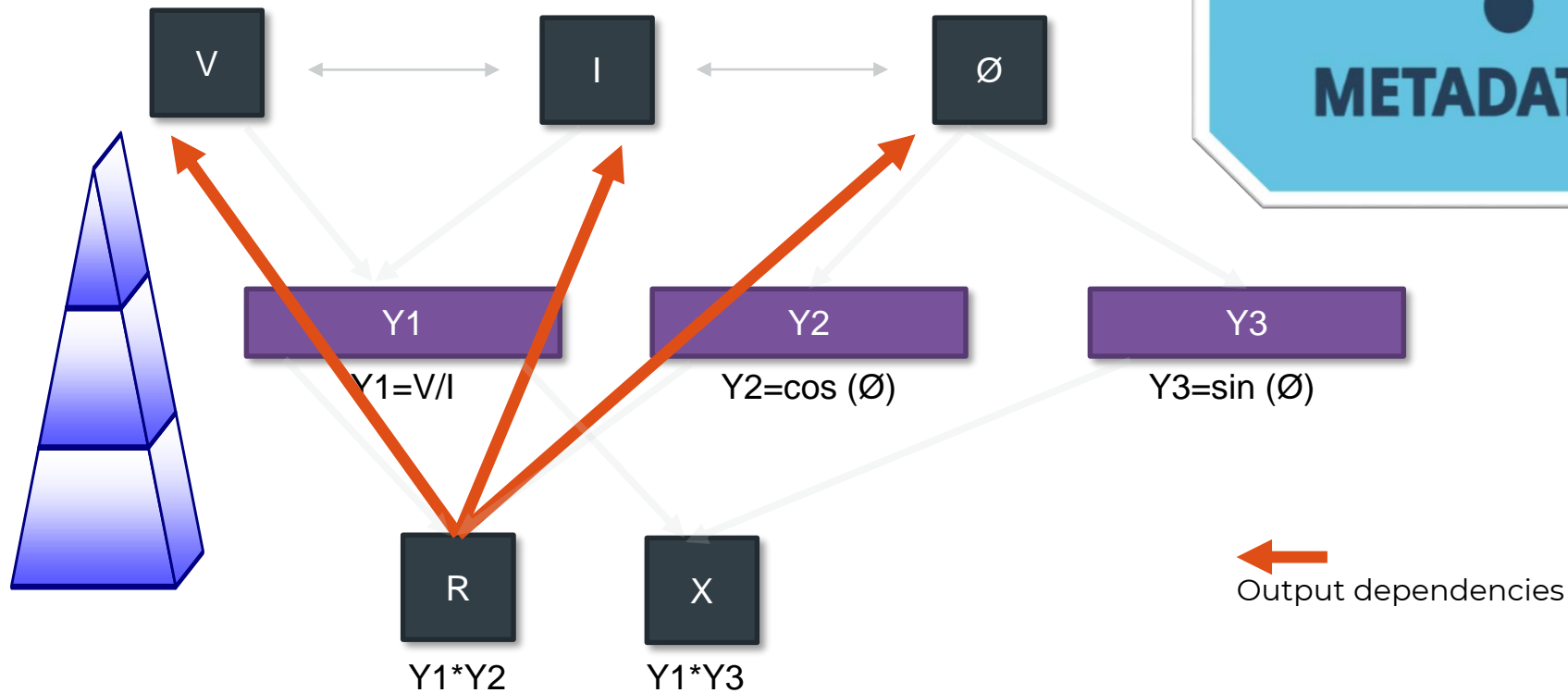
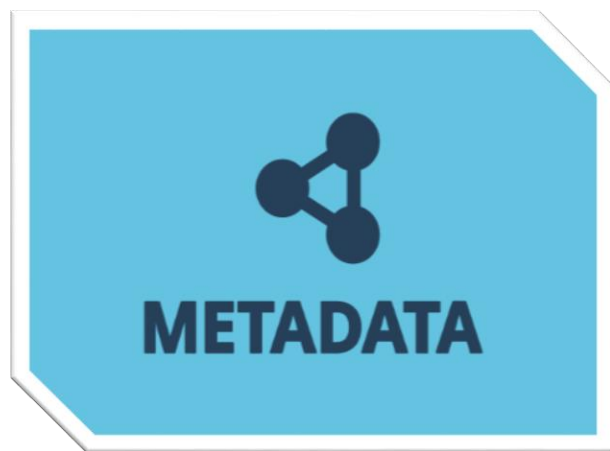
MEASUREMENT MODEL



Graphical decomposition of a measurement model

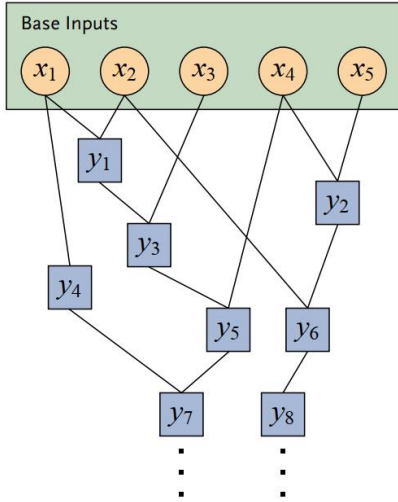
$$R = \frac{V}{I} \cos \phi$$

$$X = \frac{V}{I} \sin \phi$$



Graphical decomposition of a measurement model

Measurement Model



Issues / Solutions

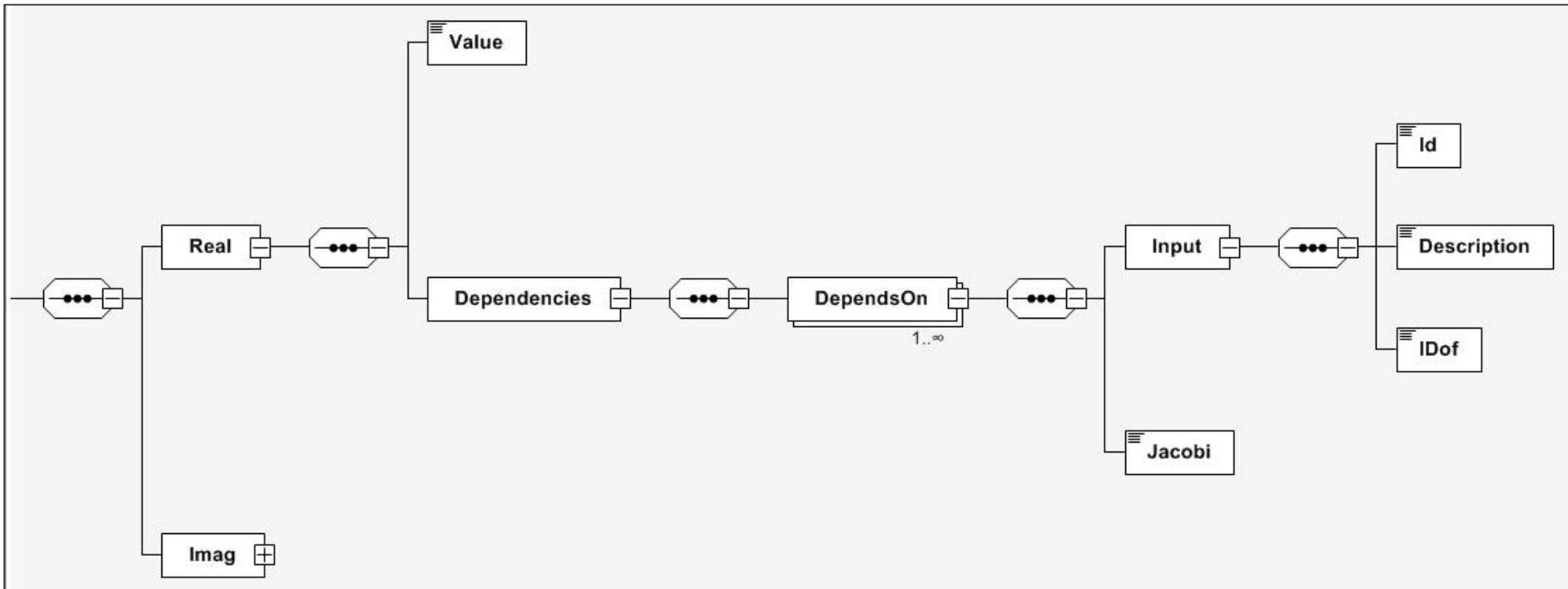
- Different models \Rightarrow Only 1 model (rigorous method)
- Mixed data types \Rightarrow Uncertainty objects
- Complicated calculations \Rightarrow Automatic uncertainty propagation through automatic differentiation
- **Lack of correlations** \Rightarrow Record of dependencies.
Correlations on demand (or explicitly saved)

Value: y_i

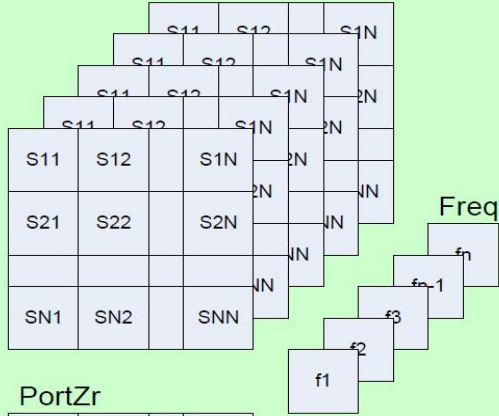
Dependencies: (x_1, x_2, x_3, \dots)

Derivatives: $\left(\frac{\partial y_i}{\partial x_1}, \frac{\partial y_i}{\partial x_2}, \frac{\partial y_i}{\partial x_3}, \dots \right)$

XSD STRUCTURE



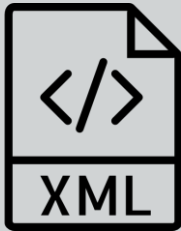
Data



Freq

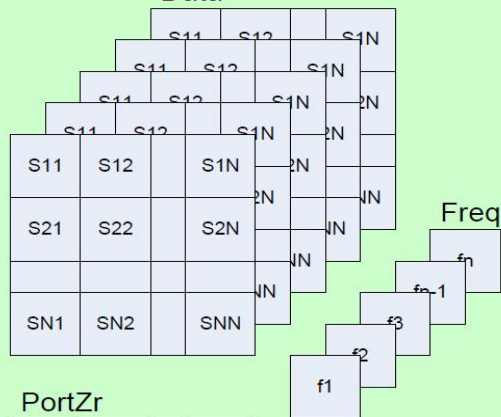
PortZr

Z1	Z2	ZN
----	----	----



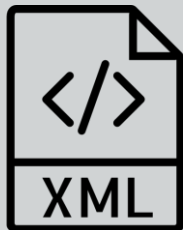
```
1 <?xml version="1.0"?>
2 <SParamData xmlns:xsd="http://www.w3.org/2001/XMLSchema" xmlns:xsi="http://www.w3.org/2001/XMLSchema-instance">
3   <FrequencyList>
218     <PortList>
219       <Port>1</Port>
220       <Port>2</Port>
221     </PortList>
222     <PortZrList>
244     <Data>
245       <Frequency>
246         <ReceiverPort>
247           <SourcePort>
248             <Real>
2189             <Imag>
4138           </SourcePort>
4139         <SourcePort>
4140           <Real>
6401           <Imag>
8678         </SourcePort>
8679       </ReceiverPort>
8680     <ReceiverPort>
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8682         <Real>
10895         <Imag>
13116       </SourcePort>
13117     <SourcePort>
13118       <Real>
15075       <Imag>
17056     </SourcePort>
17057   </ReceiverPort>
17058 </Frequency>
17059 <Frequency>
33817 <Frequency>
50599 <Frequency>
67565 <Frequency>
```

Data



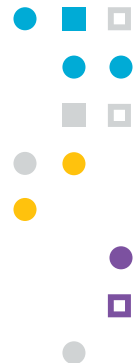
PortZr

Z1	Z2	ZN
----	----	----



```
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209 <Frequency>4825000000</Frequency>
210 <Frequency>4850000000</Frequency>
211 <Frequency>4875000000</Frequency>
212 <Frequency>4900000000</Frequency>
213 <Frequency>4925000000</Frequency>
214 <Frequency>4950000000</Frequency>
215 <Frequency>4975000000</Frequency>
216 <Frequency>5000000000</Frequency>
217 </FrequencyList>
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220 <Port>2</Port>
221 </PortList>
222 <PortZrList>
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245 <Frequency>
246 <ReceiverPort>
247 <SourcePort>
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250 <Dependencies>
251 <DependsOn>
252 <Input>
253 <Id>83-CB-32-55-4B-8C-4B-EB-91-CC-00-84-9C-4F-43-C3-00-20-00-02-00-00-01-00-76-DA-06-80</Id>
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255 <IDof>0</IDof>
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258 </DependsOn>
259 <DependsOn>
260 <Input>
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267 <DependsOn>
268 <Input>
269 <Id>83-CB-32-55-4B-8C-4B-EB-91-CC-00-84-9C-4F-43-C3-00-20-00-02-00-00-01-00-76-DA-A2-C0</Id>
270 <Description />
271 <IDof>0</IDof>
272 </Input>
```


GET_CORRELATION()



1-Port correlation @fo

	Real S1,1	Imag S1,1
Real S1,1	1,000e+000	-3,860e-002
Imag S1,1	-3,860e-002	1,000e+000

Correlación Mag 2 puertos @f

	Real S1,1	Imag S1,1	Real S2,1	Imag S2,1	Real S1,2	Imag S1,2	Real S2,2	Imag S2,2
Real S1,1	1,000e+000	-3,860e-002	3,917e-002	-5,402e-003	3,921e-002	-5,835e-003	8,870e-002	-9,785e-004
Imag S1,1	-3,860e-002	1,000e+000	3,088e-003	1,564e-001	3,204e-003	1,571e-001	-5,773e-003	3,136e-001
Real S2,1	3,917e-002	3,088e-003	1,000e+000	5,608e-001	1,000e+000	5,609e-001	9,933e-001	-7,535e-001
Imag S2,1	-5,402e-003	1,564e-001	5,608e-001	1,000e+000	5,608e-001	1,000e+000	5,772e-001	-2,250e-002
Real S1,2	3,921e-002	3,204e-003	1,000e+000	5,608e-001	1,000e+000	5,609e-001	9,933e-001	-7,535e-001
Imag S1,2	-5,835e-003	1,571e-001	5,609e-001	1,000e+000	5,609e-001	1,000e+000	5,772e-001	-2,229e-002
Real S2,2	8,870e-002	-5,773e-003	9,933e-001	5,772e-001	9,933e-001	5,772e-001	1,000e+000	-7,401e-001
Imag S2,2	-9,785e-004	3,136e-001	-7,535e-001	-2,250e-002	-7,535e-001	-2,229e-002	-7,401e-001	1,000e+000

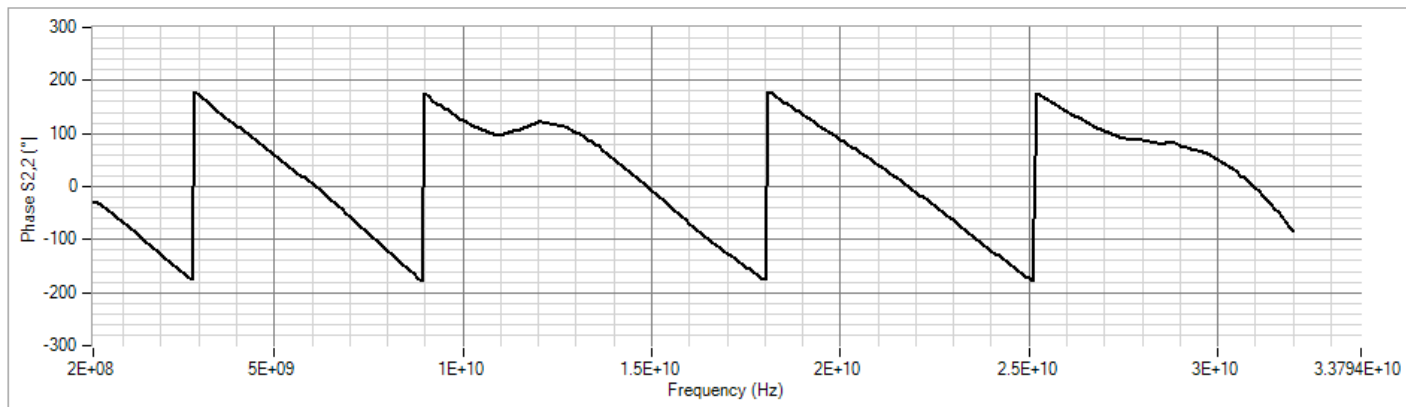
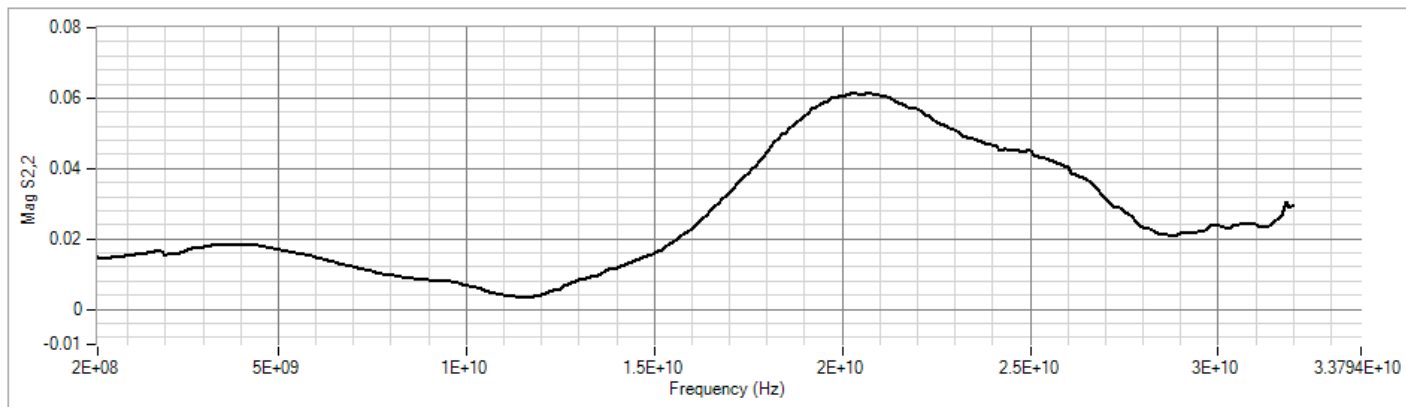
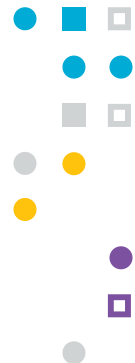


GET_CORRELATION()

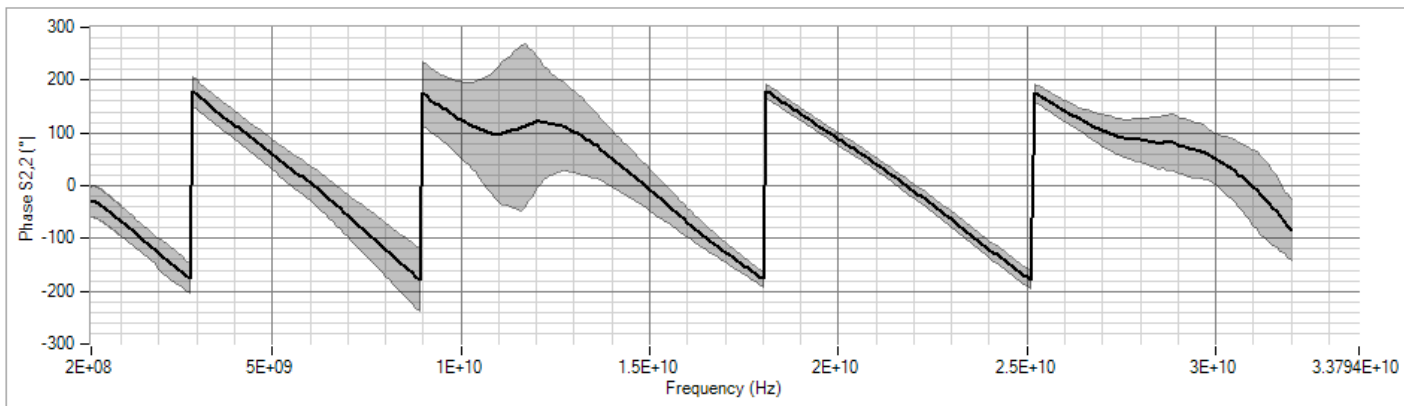
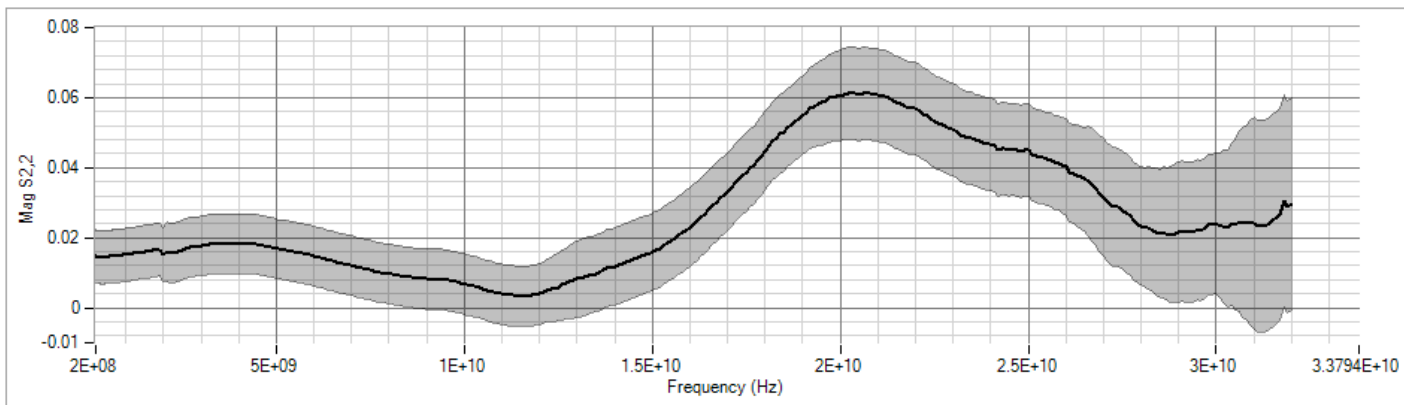
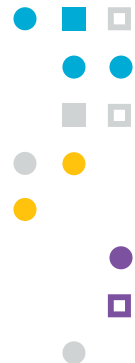
|S11| correlation between different frequencies

	95,000e+06 Hz	100,000e+06 Hz	150,000e+06 Hz	200,000e+06 Hz	250,000e+06 Hz	300,000e+06 Hz	350,000e+06 Hz	400,000e+06 Hz
45,000e+06 Hz	0,92	0,92	0,91	0,79	-0,34	0,00	0,00	0,00
50,000e+06 Hz	0,94	0,94	0,93	0,82	-0,35	0,00	0,00	0,00
55,000e+06 Hz	0,96	0,95	0,95	0,84	-0,35	0,00	0,00	0,01
60,000e+06 Hz	0,97	0,96	0,96	0,86	-0,36	0,00	0,00	0,00
65,000e+06 Hz	0,98	0,97	0,97	0,87	-0,35	0,00	0,00	0,00
70,000e+06 Hz	0,98	0,98	0,97	0,88	-0,35	0,01	0,00	0,00
75,000e+06 Hz	0,99	0,98	0,98	0,89	-0,35	0,00	0,00	0,00
80,000e+06 Hz	0,99	0,98	0,98	0,90	-0,34	0,00	0,01	0,00
85,000e+06 Hz	0,99	0,99	0,99	0,91	-0,33	0,00	0,00	0,00
90,000e+06 Hz	1,00	0,99	0,99	0,92	-0,32	0,00	0,00	0,00
95,000e+06 Hz	0,99	1,00	0,99	0,92	-0,31	0,00	0,00	0,00
100,000e+06 Hz	0,99	0,99	1,00	0,93	-0,30	0,00	0,00	0,00
150,000e+06 Hz	0,92	0,92	0,93	1,00	0,00	0,00	0,00	0,00
200,000e+06 Hz	0,32	-0,31	-0,30	0,00	1,00	0,00	0,00	0,00
250,000e+06 Hz	0,00	0,00	0,00	0,00	0,00	1,00	0,00	0,00
300,000e+06 Hz	0,00	0,00	0,00	0,00	0,00	0,00	1,00	0,00
350,000e+06 Hz	0,00	0,00	0,00	0,00	0,00	0,00	0,00	1,00
400,000e+06 Hz	0,00	0,00	0,00	0,00	0,00	0,00	0,00	0,01
450,000e+06 Hz	0,00	0,00	0,00	0,00	0,00	0,01	0,00	0,01
500,000e+06 Hz	0,00	0,00	0,00	0,00	0,00	0,00	0,00	0,01
550,000e+06 Hz	0,00	0,00	0,00	0,00	0,00	0,00	0,00	0,00

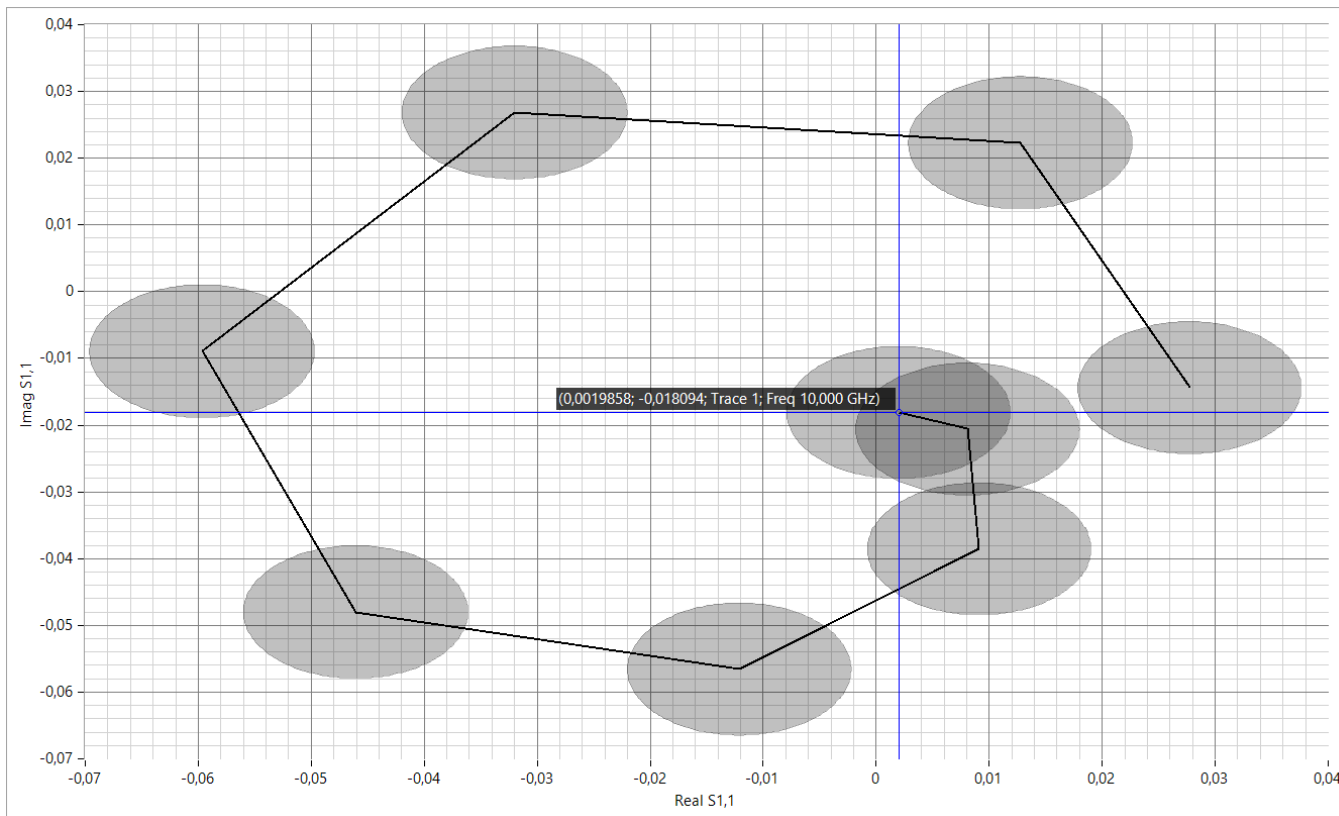
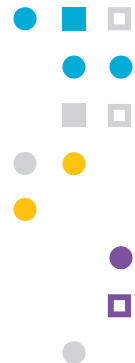
GET_VALUE(y)



GET_VALUE(y) ; GET_STDUNC(y)



Uncertainty on Complex plane 10GHz-18GHz @1GHz step



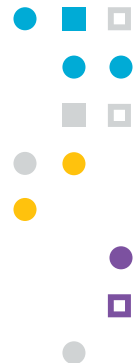
BUDGET(y)

Frequency: 2800.000 MHz, Parameter: S1,1 Zr: 50 Ω Phase (°)

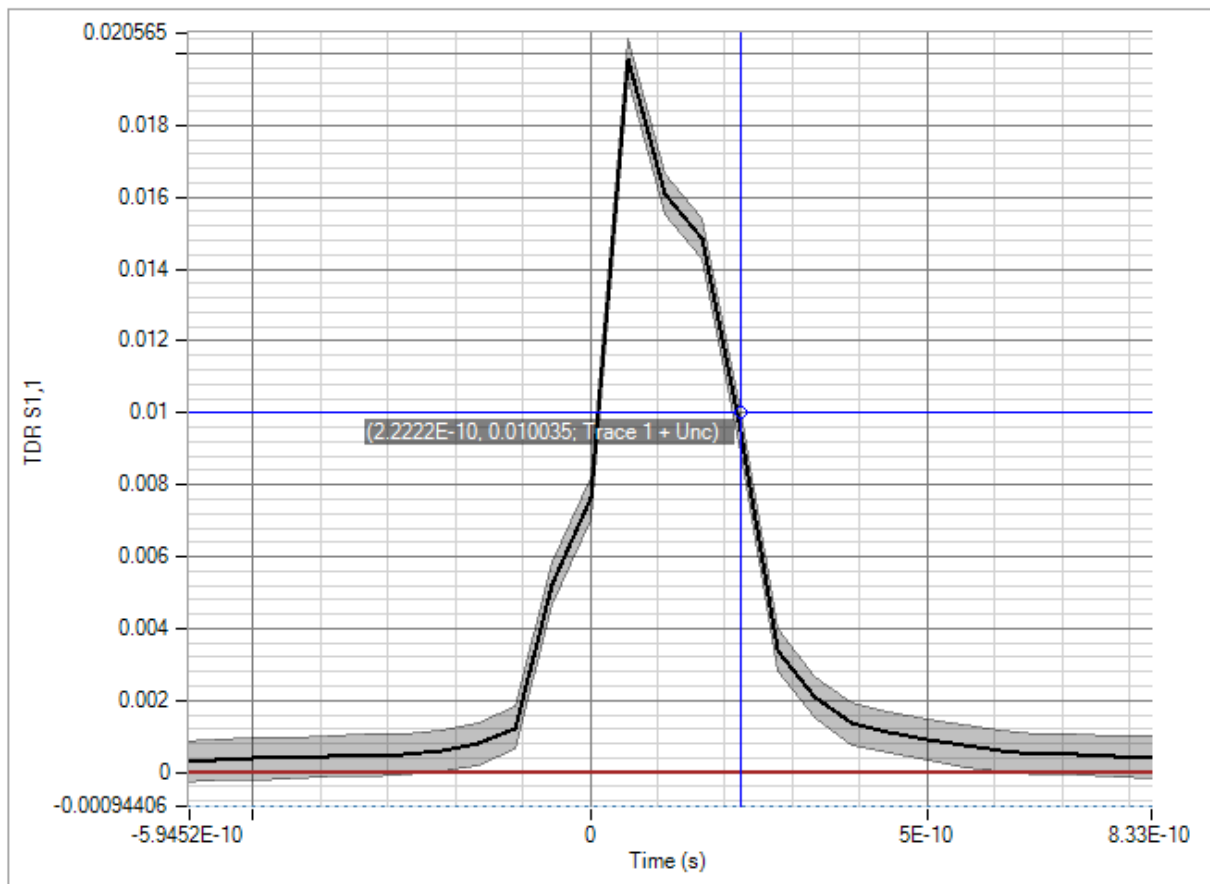
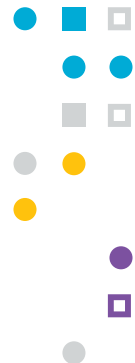
Id | Flat | Expand All | Collapse All | Numeric Format: f6 | Copy

Value	Std Unc	U95
-29.681245	29.561606	59.123212

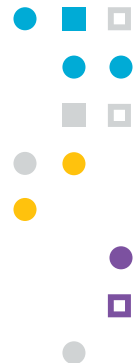
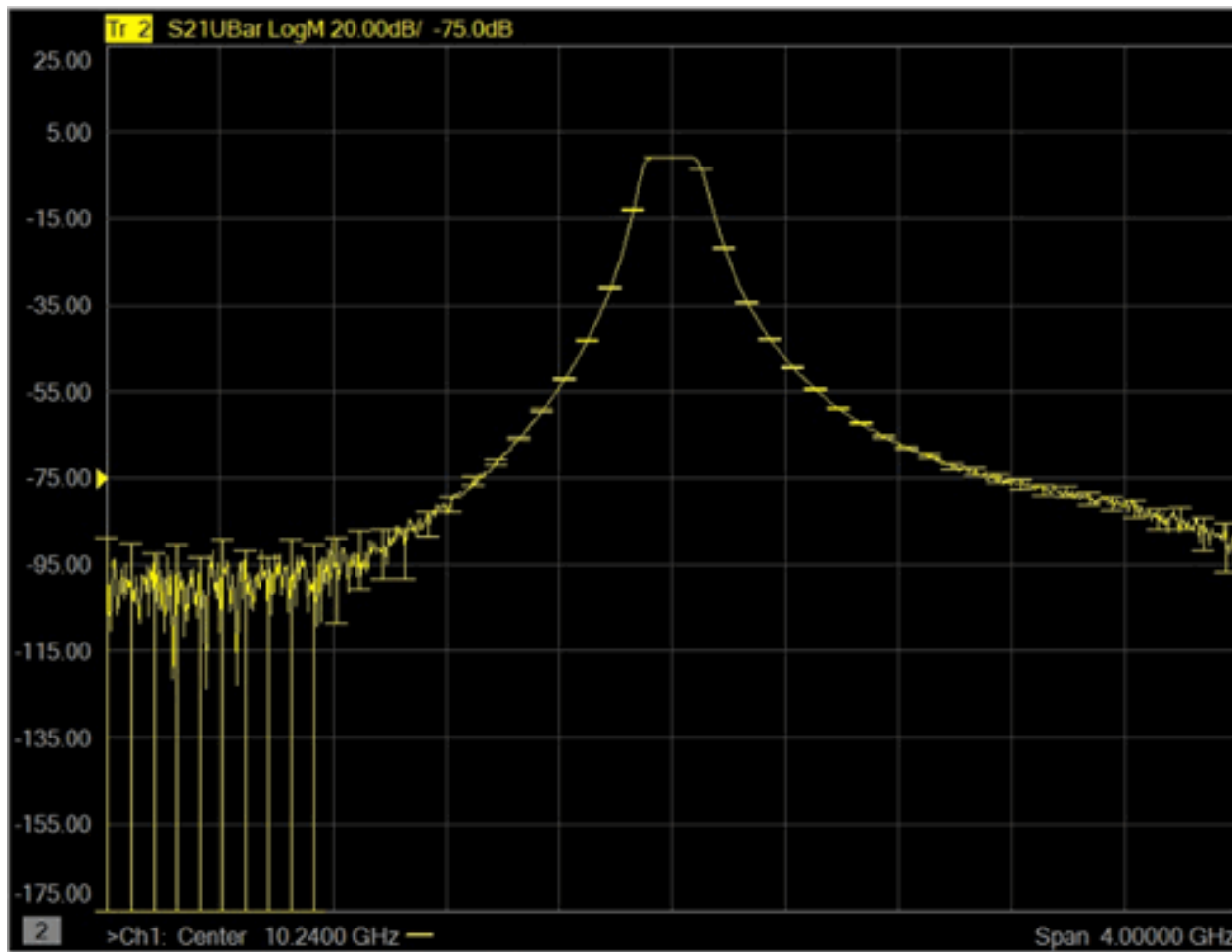
Description	Unc Component	Unc Percentage
+ Cable Stability	4.972430	2.829
- Connector Repeatability	19.795602	44.842
+ Reflection	19.795602	44.842
+ load(m)	20.925102	50.105
+ open(f)	0.222150	0.006
+ open(m)	0.121464	0.002
+ short(f)	0.222593	0.006
+ short(m)	0.120965	0.002
- VNA Drift (Ideal VNA correlated)	4.389481	2.205
+ Directivity	4.389394	2.205
+ Match	0.027649	0.000
+ VNA Linearity	0.147518	0.002
+ VNA Noise	0.141953	0.002

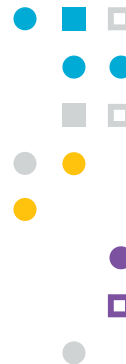


Time Domain









ROHDE & SCHWARZ

R&S ZNA-K50 Real time measurement uncertainty analysis



Maury Microwave
Your Calibration, Measurement & Modeling Solutions Partner!

MT940A Insight Calibration and Measurement software

EXAMPLE ISO-GUM H2 with GTC

INPUT
VARIABLES



```
V = ureal(4.999,3.2E-3,independent=False) # volt
I = ureal(19.661E-3,9.5E-6,independent=False) # amp
phi = ureal(1.04446,7.5E-4,independent=False) # radian

set_correlation(-0.36,V,I)
set_correlation(0.86,V,phi)
set_correlation(-0.65,I,phi)
```

MODEL



```
R = result( V * cos(phi) / I )
X = result( V * sin(phi) / I )
Z = result( V / I )
```

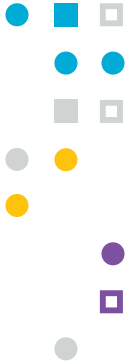
```
print 'R = {}'.format(R)
print 'X = {}'.format(X)
print 'Z = {}'.format(Z)
print
print 'Correlation between R and X = {:.2G}'.format( get_correlation(R,X) )
print 'Correlation between R and Z = {:.2G}'.format( get_correlation(R,Z) )
print 'Correlation between X and Z = {:.2G}'.format( get_correlation(X,Z) )
```

OUTPUT



```
R = 127.732(70)
X = 219.85(30)
Z = 254.26(24)

Correlation between R and X = -0.59
Correlation between R and Z = -0.49
Correlation between X and Z = +0.99
```



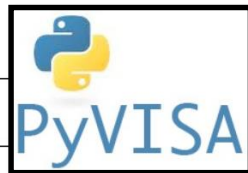
EXAMPLE ISO-GUM H2 with GTC

INPUT
VARIABLES



```
V = ureal(4.99937E-3, independent=False) # volt
I = ureal(19.661E-6, independent=False) # amp
phi = ureal(1.04446, 7.5E-4, independent=False) # radian

set_correlation(-0.36, V, I)
set_correlation(0.86, V, phi)
set_correlation(-0.65, I, phi)
```



MODEL



```
R = result( V * cos(phi) / I )
X = result( V * sin(phi) / I )
Z = result( V / I )
```

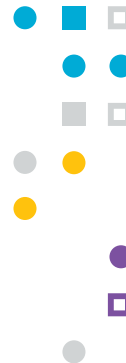
```
print 'R = {}'.format(R)
print 'X = {}'.format(X)
print 'Z = {}'.format(Z)
print
print 'Correlation between R and X = {:.2G}'.format( get_correlation(R, X) )
print 'Correlation between R and Z = {:.2G}'.format( get_correlation(R, Z) )
print 'Correlation between X and Z = {:.2G}'.format( get_correlation(X, Z) )
```

OUTPUT

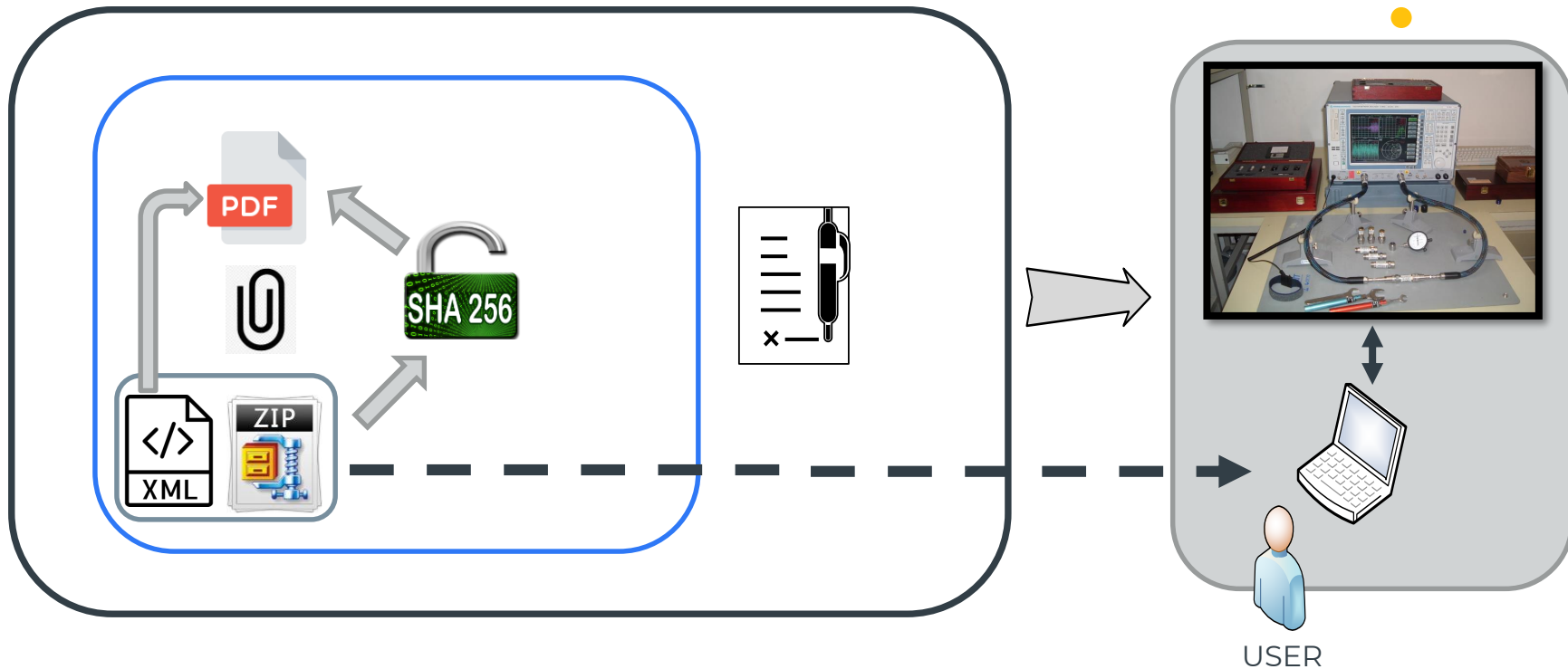


```
R = 127.732 (70)
X = 219.85 (30)
Z = 254.26 (24)

Correlation between R and X = -0.59
Correlation between R and Z = -0.49
Correlation between X and Z = +0.99
```



non-PTB DCC





Developer: Michael Wollensack

UncLib (Python)

<https://pypi.org/project/metas-unclib/>

```
pip install metas-unclib
```

UncLib (MATLAB, C#)

<https://www.metas.ch/metas/en/home/fabe/hochfrequenz/unclib.html>



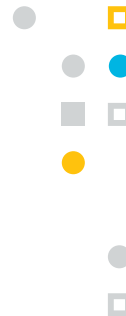
GUM TREE CALCULATOR (GTC) (Python)

Developer: Blair Hall

<https://pypi.org/project/GTC/>

<https://gtc.readthedocs.io/en/latest/install.html> (Documentation)

```
pip install gtc
```



Thank you !



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